

Mechanistic modelling of catalytic NO_x reduction reactions after hydrogen or ammonia combustion on multiple scales

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ABSTRACT

This article provides a comprehensive review and evaluation of the selective catalytic reduction (SCR) of nitrogen oxides (NO_x) using ammonia as a reducing agent in flue gases produced by the combustion of hydrogen or ammonia with air. Over the years, density functional theory calculations (DFT) have been used extensively to complement experimental results, with emphasis on understanding adsorption modes and reaction mechanisms. Recent advances in this field have led to a shift from non-periodic to more accurate periodic models. It has been shown that the SCR reactions mainly follow the Eley-Rideal mechanism, with NH₂NO identified as the most important intermediate. Global kinetic and microkinetic models are widely used, but these models often overlook the crucial role of adsorption of water molecules on catalyst surfaces. Consequently, their utility is reduced under conditions of elevated water vapor concentrations. To address this limitation, numerical fluid dynamics simulations (CFD) have been introduced that include user-defined functions to model chemical deNO_x reactions. In particular, the method CFD can also take into account the adsorption of relevant species at the active sites of the catalyst. We highlight a significant knowledge gap in the existing literature: the lack of consideration of the adsorption of water on catalyst surfaces during the selective catalytic reduction of NO_x. Consequently, these models are inadequate for flue gases with high water vapor content produced during the combustion of hydrogen or ammonia. Addressing this shortcoming is critical to better understand and accurately predict the performance of SCR under different operating conditions.

1. Introduction

The transition to a carbon-neutral society requires the decarbonization of the high-temperature heating used in many sectors (e.g. process metallurgy) [1,2], which can only be achieved by using carbon-neutral (synthetic fuels and biofuels) or carbon-free fuels. Two of the most promising carbon-free fuels are hydrogen (H₂) [3,4] and ammonia (NH₃) [5,6]. These two fuels can be used for transportation and electricity generation: H₂ has proven to be a fuel for internal combustion engines [7–10], as has a mixture of NH₃ and H₂ [11,12]; gas turbines can run on pure NH₃ [13], its mixture with H₂ [14] and on pure H₂ [15]. None of the fuels, neither H₂ nor NH₃, emit carbon dioxide or carbon monoxide during its combustion. However, combustion with air

produces NO_x emissions (a mixture of nitrogen oxide (NO) and nitrogen dioxide (NO₂) [16]; see Appendix A), which pose an environmental and health hazard.

Among other things, NO_x contributes to the formation of acid rain, which is responsible for the eutrophication of soils and water bodies and has negative effects on aquatic ecosystems as well as terrestrial vegetation [17]. Although acidic nitrate/nitric acid particles have not been shown to have direct effects on the human health [18], NO and NO₂ gases irritate the respiratory tract and cause respiratory issues via inflammation and cell damage. This makes NO_x one of the priority air pollutants for which limit values for the protection of the human health, vegetation and natural ecosystems are laid down in various directives (e.g. Directive 2008/50/EC on ambient air quality and cleaner air for Europe). Direct exposure to the more acutely toxic NO₂ can lead to

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Abbreviations			
3D	three-dimensional	N ₂	molecular nitrogen
CFD	computational fluid dynamics	N ₂ O	nitrous oxide
CHA	chabazite	NH ₃	ammonia
deNO _x	denitrification	nitro-PAHs	nitroaromatic and nitrated polyaromatic hydrocarbons
DFT	density functional theory	NO	nitrogen oxide (nitric oxide)
DOC	diesel oxidation catalyst	NO ₂	nitrogen dioxide
DRIFTS	diffuse reflectance infrared Fourier transform spectroscopy	NO _x	nitrogen oxides
EPR	electron paramagnetic resonance	NTPRD	non-thermal plasma reduction
ER	Eley-Rideal mechanism	PMoA	phosphomolybdic acid
ER	equivalence ratio	R&D	research and development
FTIR	Fourier-transform infrared spectroscopy	SCR	selective catalytic reduction
GGA	generalized gradient approximation	SNCR	selective non-catalytic reduction
H ₂	molecular hydrogen	SO ₂	sulfur dioxide
H ₂ O	water	UDF	user-defined function
IR	infrared	UV	ultraviolet
LDA	local density approximation	UWS	urea-water solution
LH	Langmuir-Hinshelwood mechanism	VOCs	volatile organic compounds
LNT	lean NO _x traps	XPS	X-ray photoelectron spectroscopy
MOFs	metal-organic frameworks	XAS	X-ray absorption spectroscopy
		XRD	X-ray diffraction
		ZSM	zeolite Socony Mobil

respiratory inflammation and reduced lung function (e.g. asthma) and increase susceptibility to other respiratory infections already at low-ppm levels [19]. However, NO_x is also harmful because of its indirect effects on the ecosystem, human health and climate. Photolysis of NO₂ leads to the formation of toxic ozone in the lower atmosphere and, in combination with volatile organic compounds (VOCs), to the formation of photochemical smog, which is particularly harmful to health [20], but also reduces visibility and contributes to climate change. Nitrogen oxide species in the atmosphere react with other air pollutants to form, for example, nitroaromatic and nitrated polyaromatic hydrocarbons (nitro-PAHs), which are highly toxic, carcinogenic and mutagenic to humans and other living organisms [21–23]. In particular, nitrated (poly)aromatic pollutants are also strong absorbers of the near UV radiation and visible light, which causes atmospheric heating and climate change [24].

Therefore, in addition to decarbonization, there is a global need to reduce the combustion emissions of NO_x into the atmosphere, including emissions from the combustion of ammonia and/or hydrogen (with air), which can be achieved by selective catalytic reduction of nitrogen oxides (SCR deNO_x). Alternative ways to reduce nitrogen oxide emissions include avoiding their formation during combustion through (i) oxyfuel combustion (combustion in a near-pure oxygen environment) [25,26], (ii) optimized burner design and proper combustion management [15, 27,28] and (iii) catalytic combustion e.g. catalytic hydrogen combustion (CHC) [29]. Examples of alternative post-combustion reduction technologies include (i) selective non-catalytic reduction (SNCR), which includes the injection of a reagent at high temperatures (between 850 and 1175 °C) [30,31], (ii) NO_x storage in lean NO_x traps (LNT), which includes NO_x reduction during the periods of rich exhaust gas conditions typically used with hydrocarbon fuels, e.g. diesel [32,33] and (iii) NO_x removal by non-thermal plasma reduction (NTPRD), which necessitates electrical power source to operate [34,35]. However, these alternative NO_x emission reduction methods involve high operating costs (oxyfuel combustion), require research and development (R&D) and investments for infrastructure modifications (optimized or catalytic combustion), or are not applicable to carbon-free fuels (LNT).

1.1. Formation and selective catalytic reduction of nitrogen oxides

During combustion, nitrogen from the air (or the fuel itself) can be converted into nitrogenous pollutants such as NO, NO₂, N₂O, NH₃. The

species formed and their ratios depend on the combustion conditions, e.g. temperature, air-to-fuel ratio, pressure, etc. N₂O emissions are usually insignificant because N₂O reacts rapidly with the H and OH radicals to form N₂ or decomposes by itself in colder regions downstream of the flame [16]. On the other hand, the formation and decomposition processes of NO_x during combustion are very complex. There are three different pathways of the NO formation: (i) oxidation of atmospheric nitrogen (with O, O₂ and OH; the Zeldovich mechanism) - thermal NO, (ii) reactions of atmospheric nitrogen with hydrocarbon radicals (mainly HCN; described by Fenimore) - prompt NO and (iii) oxidation of nitrogen bound in the fuel (with O₂; Pershing and Wendt) - fuel NO [16]. NO₂ forms from NO, which usually occurs in the areas, where rapid cooling takes place (e.g. in the area where hot combustion gases mix with the inlet air [16]). Typically, NO_x emissions in the combustion products consist of 90 vol% NO and 10 vol% NO₂ [36].

SCR deNO_x is a process of converting NO_x from flue gases to nitrogen (N₂) and water vapor using a reducing agent and a catalyst. The most commonly used reducing agents for the SCR deNO_x process are NH₃ and urea-water solution (UWS). Alternative reducing agents for SCR deNO_x are: H₂ [37], hydrocarbons, alcohols, carbon monoxide [38] and others. Since most of the research and development work is concentrated on SCR deNO_x with ammonia (NH₃-SCR deNO_x), this paper focuses on these processes.

There are three main SCR deNO_x reactions with ammonia in a lean environment (excess oxygen during combustion, which is also present in a flue gas).



The reaction (1.1) is usually referred to as the standard SCR reaction. The fastest and preferred SCR reaction is reaction (1.2). To promote reaction 1.2 (rapid SCR reaction), the molar ratio between NO and NO₂ should be close to one. Since NO usually predominates, this could be achieved by pre-oxidizing a portion of NO to NO₂ (using a separate catalyst, e.g. diesel oxidation catalyst (DOC), or on the SCR deNO_x

catalyst itself [39]). The reaction 1.3 (NO₂-SCR reaction) occurs when excess NO₂ is present. NO₂ can also react (reaction 1.4) to form N₂O, which is an undesirable side reaction between ammonia and NO₂ because the resulting N₂O has a greenhouse effect and depletes the stratospheric ozone layer [40].



Insufficient mixing, excess ammonia, or a rapid release of the stored ammonia (through the catalyst) can cause ammonia emissions, which is known as an ammonia slip. This becomes a problem when high NO_x conversions (>90%) are required. Therefore, ammonia slip catalysts (ASC) are commonly used in vehicle exhaust treatment systems to oxidize excess ammonia to harmless nitrogen and water vapor [40].

The presence of SO₂ and/or water vapor in exhaust gases inhibits SCR deNO_x processes due to the effect of SO₂ and H₂O poisoning [41, 42]. Hydrogen and ammonia are sulfur-free and the deNO_x catalysts are not poisoned by SO₂. However, water vapor would be present in large quantities. Stoichiometric combustion of hydrogen and ammonia with air produces flue gases with 34.7 vol% and 31.1 vol% water vapor, respectively (Appendix B: Tables B.1 and B.2). Even if the equivalence ratio is increased to 1.25 (lean combustion), the combustion products would contain 28.8 vol% and 26.3 vol% water vapor, respectively.

1.2. Water vapor inhibition effects on the NH₃-SCR deNO_x processes

There are two main mechanisms of the H₂O-induced inhibition of the NH₃-SCR deNO_x reactions and the corresponding catalyst poisoning. The first is hydroxylation of the catalyst surface in the presence of large amounts of water, which reduces the number of available active sites on the catalyst. This is an irreversible process during catalyst operation, as activity is only restored at dehydration temperatures above 350 °C. Moreover, the competing adsorption of H₂O and NH₃ decreases the adsorption capacity for NH₃, which lowers the reaction rate and inhibits the deNO_x process SCR [43].

Some authors [44,45] claim that the inhibition of SCR deNO_x by water vapor is proportional to the water vapor content up to 5 vol% and then flattens out, as shown in Fig. 1.

Yun and Kim [46], on the other hand, have predicted a significant reduction in the NH₃-SCR deNO_x performance of a commercial V₂O₅ catalyst even at higher water vapor content, which is shown in Fig. 2. These discrepancies could originate from the differences in experimental

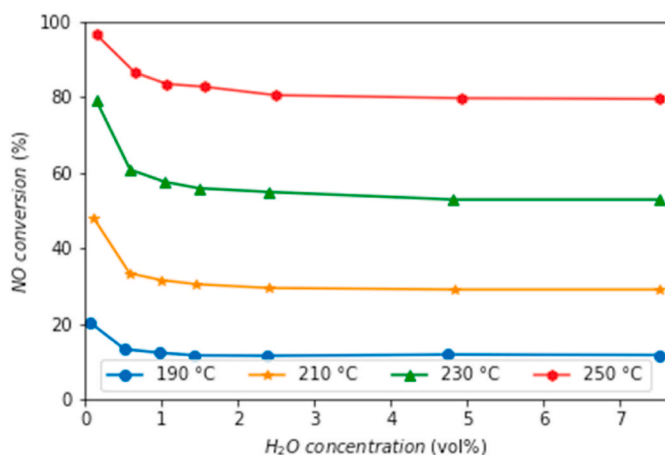


Fig. 1. Effect of water vapor on NO conversion over vanadia-based commercial catalyst (ZERONOX®, Katalysatorwerke HiJls GmbH; 0.4 g of catalyst at 180–300 μm sieve fraction) at various temperatures. Adapted from Ref. [44]. Feed gas mixture: 10 vol% O₂, 1000 ppm NO, 1000 ppm NH₃, 0 to 7.5 vol% H₂O, balance N₂ at flow rate of 500 ml/min. Copyright © 1996 Published by Elsevier Ltd.

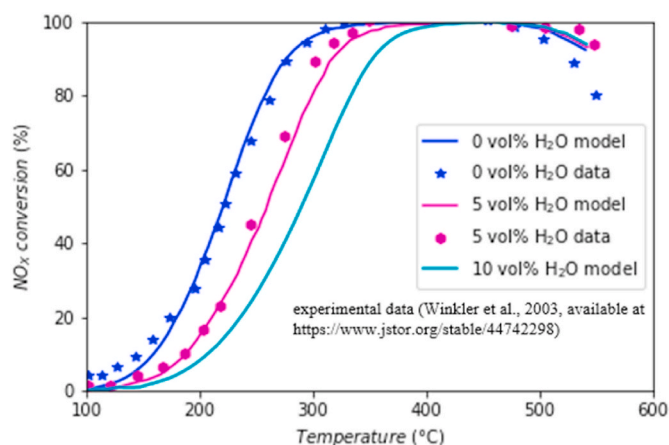


Fig. 2. Influence of H₂O content on the NO_x conversion of a commercial V₂O₅ catalyst (the sample with diameter and length of 1 inch including a 400/4 [psi/mil] substrate coated with a vanadium-based washcoat). Adapted from Ref. [46]. The exhaust gas contained 2 vol% O₂, 500 ppm NO and 500 ppm NH₃, H₂O concentration was varied; It was fed to the SCR catalyst at the space velocity of 20,000 h⁻¹. Copyright © 2012 Elsevier Ltd.

conditions: simulated flue gas composition, composition and form (powder versus monolith) of a catalyst sample, pretreatment procedure of gases (e.g. preheating, mixing), sampling and characterization of gases and others.

However, most authors tested catalysts only at low water vapor concentrations in flue gases, usually below 5 vol% [47] and occasionally up to 10 vol% in simulated flue gases [48]. Therefore, the effect of water vapor on the NO_x conversion efficiency at high water content (>15 vol %) is currently unknown.

On the other hand, water vapor may also have a promoting effect on NH₃-SCR deNO_x performance under certain conditions (at H₂O contents below 5 vol%). It can inhibit N₂O formation (enhanced N₂ selectivity), catalyse the transition from Lewis acid sites to Brønsted acid sites and facilitate the production of SCR-reactive intermediates [49]. Both, the promoting and inhibiting effect of H₂O coexist, and the overall effect depends on the water vapor concentration.

1.3. Catalyst materials, characterization and measurement methods

It is difficult to identify the best catalyst for a process as there is usually no single catalyst that gives optimal results under all operating conditions. Therefore, over the years, numerous catalytic materials have been investigated for their activity (and stability) in SCR deNO_x. In the past, commercial SCR deNO_x catalysts used to be based on noble metals, such as Rh, Pt and Pd on a metal oxide matrix support (CeO₂, ZrO₂, Al₂O₃ and others) [50]. Current catalytic materials are based on either (i) metal oxides of copper, nickel, iron, vanadium and other transition metals or on (ii) metal ion-exchanged zeolites, mainly Cu- and Fe-exchanged zeolites [51]. Recently, a patent has been published (WO 2019/166267) using a zeolite-based material loaded with iron. Also, the commercial material REMEDIA® has been shown to remove dioxins and NO_x [52]. In some cases, copper-loaded vanadia and TiO₂ materials have also been used for NO_x abatement [50,53,54]. In recent years, increased attention has been given to Mn-based materials [55–57], since several issues plague the vanadium-based catalyst. Since the materials require a higher operating temperature, they are installed up-stream of the exhaust. The latter leads to several issues, such as deactivation of the materials due to coke deposition, poisoning by SO₂, etc. [58,59].

There are several material properties that determine the catalyst performance. These are usually input data for modelling and predictive studies and must be accurately selected and determined to obtain reliable computational results. The number of active sites and their surface

distribution are essential information for kinetic studies. However, any additional experimental information (e.g. the strength of reactant binding, different types of active sites) drastically improves the accuracy of the developed model.

There are numerous characterization techniques that are ubiquitous in catalyst research, such as powder X-ray diffraction (XRD) and sorption of probe molecules (e.g. N_2 , H_2 and CO) [60–62]. These methods provide general information about the catalyst structure (crystallinity) and its surface, which is necessary for the development of a microkinetic model. A very useful complementary technique is chemisorption of reactants, which can provide specific information about the active phase of the catalyst, including the binding strength of reactants and/or products. Competitive adsorption of potential spectator molecules of catalyst poisons is also an important approach, that can be used to evaluate the effect of a poison on catalyst activity [61,63,64]. The amount and the inferred nature of binding provide essential information about the poisoning effect, which is often a bottleneck in catalyst selection. In this regard, X-ray photoelectron spectroscopy (XPS) and diffuse reflectance infrared Fourier transform spectroscopy (DRIFTS) provide complementary information about the binding of molecules and their chemical environment, especially with respect to the oxidation state of the active site. Another very accurate technique that is not widely available is X-ray absorption spectroscopy (XAS). This technique can be used to study the active site at the atomic level, which in combination with DFT calculations can lead to improvements in determining the reaction mechanism [65].

There are many other analytical techniques used in the characterization of catalysts, which have already been described in detail in another review [66]. We mention here only those most commonly used in SCR deNO_x research and would like to emphasize that a combination of different characterization techniques and catalytic tests gives the most accurate results. In this context, a post-mortem catalyst analysis with Mössbauer spectroscopy combined with electron paramagnetic resonance (EPR) used by Grünert et al. [67], has shown that Fe^{III} are the most active sites for NO_x abatement.

1.4. Outline of the paper

This paper is a review of recent advances in the field of mechanistic modelling of SCR of NO_x emissions from flue gases, with emphasis on the treatment of flue gases produced during the combustion of hydrogen or ammonia. The article consists of (i) an introduction explaining the problems associated with nitrogen oxide emissions and methods to reduce them, focusing on NH₃-SCR deNO_x and a description of typical catalyst materials, their characterization and methods to evaluate their performance, (ii) an overview of the SCR deNO_x models at the atomistic scale, (iii) a description of global kinetic and microkinetic models, (iv) a description of SCR catalysis by computational fluid dynamics (CFD), (v) conclusions with a brief summary of the current state of research on the models and a future outlook.

2. Atomistic-scale DFT modelling

Due to the complexity of the reaction network in SCR deNO_x reactions, few first-principles reaction models have been established and investigated using DFT calculations. More often, a reaction mechanism is postulated and experimental data are fitted using microkinetic models that provide phenomenologically optimized kinetic parameters. DFT calculations are mostly used to support experimental data and are limited to adsorption energies, charge transfer and structural properties. The notorious problem remains model construction, which must be computationally tractable, yet physically meaningful. Conventional characterization methods, such as XRD, XPS, IR spectroscopy etc. are used to obtain information about the structure of the material, which is then used as input in modelling.

Structure-activity relationships are highly sought after in the

optimization of SCR catalysts. In this chapter, we give an overview of the few first-principles attempts to describe these reactions. Although there are several variants of DFT, computational feasibility and chemical accuracy have reduced the useful approaches to a handful. The generalized gradient approximation (GGA) is most commonly used because it is not much more costly than the local density approximation (LDA) but considerably more accurate. To account for *d* electrons of Ti and V, the Hubbard-like DFT+U approach is usually used. Hybrid-functional realizations of DFT are used only for single point calculations on pre-optimized structures due to their extreme computational costs, although they provide superior electronic properties, very accurate adsorption energies and reaction barriers. Even more expensive methods, such as coupled clusters, are used only to evaluate the accuracy of different lower-level approaches on isolated species, such as on O=V(OH)₃ and O=VSi₇O₁₂H₇ [68]. In all cases, periodic calculations are preferred to describe heterogeneous catalysts with a repeating structure. Depending on the purpose of the DFT calculations, different quantities are calculated: (i) geometrical structures, (ii) electronic properties, (iii) adsorption strength, (iv) reaction kinetic parameters. Most simulations focus on (i) and (iii) and consider (ii) only indirectly, while (iv) is almost completely disregarded.

2.1. Structure and electronic properties

Although this is a prerequisite for any DFT calculation, in this section we explicitly list the works where the calculation of the structure and electronic properties is the most important insight offered by DFT. This is usually done to support FTIR, DRIFTS or Raman measurements, or to compare charge transfer and similar quantities with observed reaction performance. Therefore, these studies remain descriptive.

2.1.1. Ceria-based catalysts

Yan et al. [69] investigated Nb-modified SnO₂-CeO₂ catalysts and used DFT calculations to determine the charge distribution and partial electronic charge on the catalyst surfaces as well as the band structures. They also investigated the energy of oxygen vacancy formation. Similarly, Mu et al. used DFT to study the charge interaction between Fe and V in FeVO₄ [70].

Nolan et al. focused on the electronic structure and molecular adsorption of NO₂ and O₂ on ceria with different oxygen oxidation numbers [71–73]. Joshi et al. further demonstrated the positive effect of tungsten doping [74].

2.1.2. TiO₂-based catalysts

To support the DRIFTS measurements, Huan et al. also calculated the adsorption of NO, NH₃, NO₂, O₂ and N₂ on TiO₂(001) and TiO₂(101) [75]. Experimental studies on Sm and Zr doping of MnO_x-TiO₂ catalysts were elaborated by Sun et al. [76] using DFT to calculate differential charge densities or deformation electron density and the density of states during adsorption [77]. For MnO_x-FeO_y nanocage catalysts, Yan et al. [78] used DFT only to evaluate the charge density transfer.

Occasionally, DFT simulations are used in design studies, as shown by Peng [79], who calculated the electronic properties of differently doped TiO₂ to evaluate its redox potential. Very rarely, authors use DFT models to explain Raman spectra, as Due-Hansen et al. did for vanadia-based catalysts on wolframated and sulphated zirconia [80].

2.2. Adsorption

Historically, adsorption has been the most common DFT result, such as in the seminal work by Yin et al., in 1999 [81]. Nowadays, adsorption is most often evaluated to explain the experimental data characterizing a catalyst, to provide clues about the reaction mechanism and/or the intermediates involved, or to study the catalyst poisoning. In general, authors calculate the adsorption energies, omitting entropy effects and foregoing the analysis of the Gibbs free energy of adsorption (except

when studying phase diagrams). Therefore, the adsorption energy calculations are used to make comparisons and show trends, but not to predict the catalyst coverage at different operating conditions. This is understandable since the exact catalyst surface area is often unknown or too variable to be suitable for DFT.

2.2.1. Ceria-based catalysts

Peng et al. [82] studied NH_3 adsorption on differentially doped (Fe, Mn, La, Y) CeO_2 catalysts and found that it improved with all dopants. The inherent limitations of modelling are perhaps best illustrated by Maitarad et al. [83], who used to $\text{CeO}_2(110)$ and $\text{Mn@CeO}_2(110)$ to describe the $\text{MnO}_x/\text{Ce}_{0.9}\text{Zr}_{0.1}\text{O}_2$ material while investigating NH_3 adsorption energies and oxygen vacancy formation energies.

Sulfur poisoning of CeO_2 was attributed to the formation of SO_x surface species [84], which is also true for Mn-doped CeO_2 [85]. In the latter case, the authors performed an extensive DFT study, including first-principles phase diagram calculation, which is rarely done, e.g. for Cu-SSZ-13 by Kerkeni et al. [86].

2.2.2. TiO_2 -based catalysts

More extensive studies, such as that of Huang et al. [75] on $\text{TiO}_2(001)$ and $\text{TiO}_2(101)$, investigate the adsorption of several gases involved: NH_3 , NO , NO_2 , N_2 , O_2 . Except for NH_3 , all other gases were found to be purely physisorbed.

Cheng et al. used DFT, to evaluate the adsorption energy of ammonia on Nb-promoted iron titanate and explain the results of DRIFTS [87]. Similarly, Liu et al. [88] investigated the adsorption of NH_3 and NO on $\text{Fe}_2\text{O}_3/\text{TiO}_2\{001\}$ and $\text{Fe}_2\text{O}_3/\text{TiO}_2\{101\}$ and confirmed the superior activity of $\text{TiO}_2\{001\}$, while Song et al. investigated monomeric vanadium oxide supported anatase (TiO_2) [89]. Since water desorption is often the rate-determining step, several studies focused exclusively on water adsorption, e.g. by Broclawik [90] on W-doped V_2O_5 clusters.

One of the few deactivation studies using DFT [91] showed that arsenic-induced poisoning of a commercial catalyst ($\text{V}_2\text{O}_5\text{-WO}_3/\text{TiO}_2$) was due to the formation of unreactive As-OH groups. DFT was used to calculate adsorption energies and charge transfer.

Conversely, Yu et al. [92] showed that SO_2 has a positive effect on Pb-poisoned $\text{V}_2\text{O}_5\text{-WO}_3/\text{TiO}_2$, which they confirmed by calculating SO_2 and NH_3 adsorption on the surface. Peng et al. studied NH_3 adsorption on pristine TiO_2 , Mn-substituted TiO_2 and K-doped TiO_2 to evaluate the effects of poisoning [93] and discovered that it was due to the decrease in surface acidity, loss of reducibility and the enhancement of stable nitrite/nitrate species. Similarly, $\text{V}_2\text{O}_5/\text{TiO}_2$ catalysts doped with MoO_3 and WO_3 were tested for As poisoning [94].

2.2.3. Zeolite-based and other catalysts

The adsorption and dissociation energies of NH_3 , including NO- and O_2 -assisted pathways, were calculated by Paolucci on Cu-SSZ-13 and compared with operando spectroscopy measurements [95]. The position and oxidation state of the Cu atom in SSZ-13 was then studied in more detail by Borfecchia et al. [96]. Cu-SSZ-13 has been investigated in countless DFT studies, but most of them involved structural calculations with non-periodic [97–106] or periodic models [107–110]. Similarly, MOFs can also act as catalysts, which led Zhang et al. to investigate the adsorption of the involved gases in Mn-MOF-74 [111].

Chen et al. described $\text{Co}_{0.5}\text{Mn}_1\text{Fe}_{0.25}\text{Al}_{0.75}\text{O}_x\text{-LDO}$ as CoMn_2O_4 (311) when evaluating adsorption energies of NH_3 , NO and NO_2 [112]. In PMoA clusters, co-adsorption interactions are important, as shown by Jia et al. [113].

Fan et al. [114] discovered new active sites for SCR on the (001) facet of $\alpha\text{-Mn}_2\text{O}_3$, which is more active than the traditional (111) facet. DFT confirmed this is caused by charge redistribution on the surface, which facilitates the adsorption of NH_3 on the (001)-Mn3-terminated surface. MnFeOx nanostructures, such as Dy-doped nanowires [115] or Nb- and Nd-doped nanobelts [116], are also active in SCR due to their strong adsorption of NH_3 , as shown by DFT calculations and charge difference

analysis.

2.3. Reaction mechanism

Studies of the reaction mechanism are somewhat less common and are usually purely theoretical studies with little to no experimental support. The first study that explicitly investigated the reaction mechanism by calculating transition states was done in 2003, when Anstrom et al. constructed a $\text{V}_4\text{O}_{16}\text{H}_{12}$ cluster to simulate the $\text{V}_2\text{O}_5(010)$ surface [117]. It was found that NH_4 and NO react to form NH_3NHO , convert to NH_2NO by transferring two hydrogen atoms to the $\text{V}=\text{O}$ groups and isomerise to various NH_2NO species (NH_2NO , *trans*- $\text{NH}=\text{NOH}$, *cis*- $\text{NH}=\text{NOH}$, *cis*- $\text{HN}=\text{NO-trans-H}$). The rate of the SCR reaction is determined by the formation of NH_2NO and not its isomerization. Soyer et al. studied a similar mechanism on a $\text{V}_2\text{O}_9\text{H}_8$ cluster representing $\text{V}_2\text{O}_5(010)$ [118].

2.3.1. TiO_2 -based catalysts

In 2005, Vittadini established one of the first periodic models and described the reaction on $\text{TiO}_2(001)$ [119]. The study by Calatayud et al. is noteworthy because it calculated the whole mechanism on different vanadium oxide clusters and periodic models of vanadium-substituted $\text{TiO}_2(001)$, considered the reoxidation of the catalyst and compared the results with experiments [120].

Arnarson et al. [121] studied the reaction mechanism with DFT on $\text{VO}_x/\text{TiO}_2(001)$ catalysts (Fig. 3), including the standard and the fast catalytic reduction reactions. In both cases, NH_3 binds to a V^{5+} active site and reacts with NO . Both cycles (NO-activation and fast SCR) play an important role and have the same reduction part but differ in the active oxidant (NO_2 or $\text{NO} + \text{O}_2$). At low temperatures, the standard reaction rate of SCR is determined by the formation and desorption of H_2O . The fast SCR reaction employs NO_2 directly, making the conversion faster. At higher temperatures, the reaction rates are determined by the reduction, which is the same for both pathways. While Arnarson et al. used isolated V species on titanium dioxide, He et al. [122] showed that the use of polymeric vanadyl species improves the catalyst activity due to lower reaction barriers and a smaller number of reaction steps. In all cases, no higher level modelling was performed and only DFT was used to arrive at conclusions. In their seminal work, He et al. [122] showed experimentally and theoretically with full mechanistic evaluation that polymeric vanadyl species are superior to monomeric vanadyl species.

On $\text{MnO}_x/\text{TiO}_2$, Wei et al. analyzed the three reaction steps: reaction at the Lewis acid site, reaction at the Brønsted acid site and regeneration (oxidation) of the catalyst [123], which are shown in Fig. 4.

Yuan et al. constructed various V_2O_5 -based catalytic surfaces and calculated three complete mechanisms: the Lewis acid mechanism, the Brønsted acid mechanism and the nitrite mechanism [124]. They confirmed that the latter two mechanisms compete with each other, while the Lewis acid mechanism does not match experimental observations in terms of the reaction order.

2.3.2. Zeolite-based catalysts and metal-organic frameworks

On Fe-exchanged zeolites, Li and Li investigated the possible reaction mechanism for the rapid SCR reaction using DFT [125]. When investigating the reaction of NO and NO_2 (bound as N_2O_3) with NH_3 in (i) the gas phase and (ii) on zeolites and (iii) the decomposition of NH_4NO_2 , the reaction barrier was calculated to be 22.5, 24.0 and 21.2 kcal/mol, respectively. Therefore, Chen et al. focused on oxygen dissociation via $(\text{NH}_3\text{-Cu-NH}_3)^+$ in Cu-CHA [126], and calculated the phase diagram of $\text{Cu}(\text{NH}_3)_x^+$ in CHA as a function of NH_3 pressure and temperature, as well as the thermodynamics and kinetics of O_2 activation. Moreno-González calculated the entire reaction pathway on Cu-CHA [127] and found that the activation barriers in the direct oxidation of dimers are only 70 kJ/mol. Barriers of over 2 eV were calculated for Cu-SAPO-18 [128].

Recently, metal-organic frameworks, such as manganese- or iron-

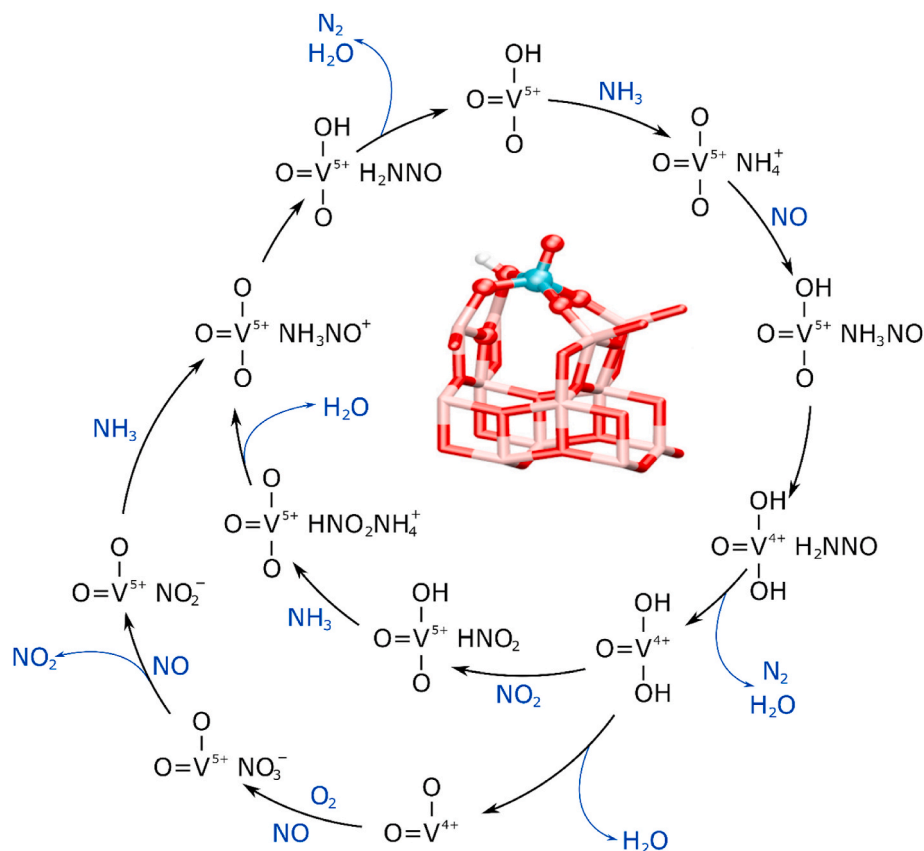


Fig. 3. A reaction mechanism of the SCR process on a VO_x/TiO₂ catalyst, as revealed by DFT calculations. Adapted from Ref. [121]. © 2017 Elsevier Inc.

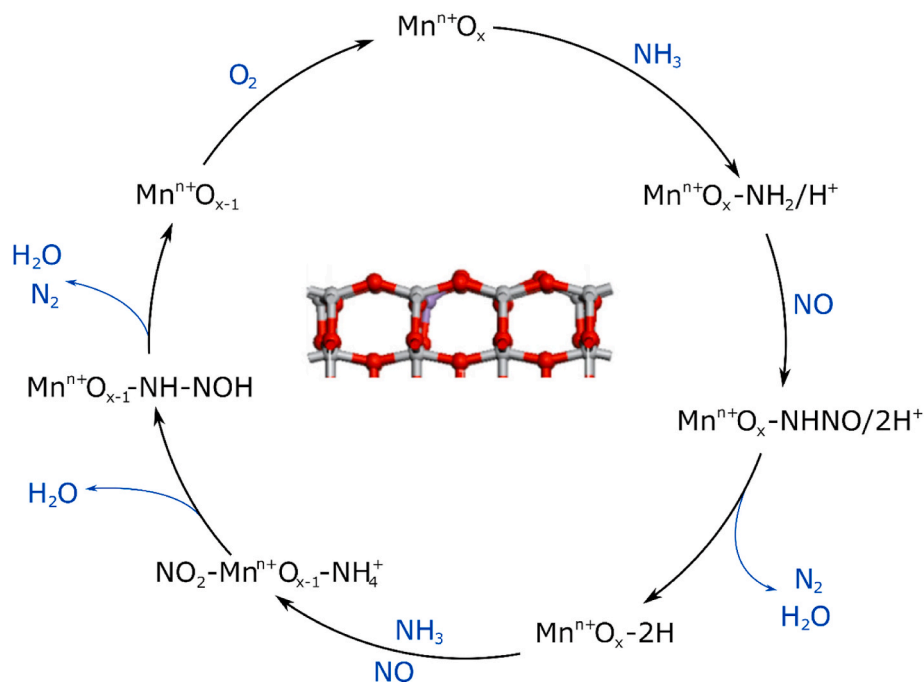


Fig. 4. NH₃-SCR reaction path over MnO_x/TiO₂ catalyst discovered via DFT calculation. Adapted from Ref. [123]. © 2017 Elsevier B.V.

based BTCs (1,3,5-benzenetricarboxylate), have seen increased interest in mechanistic studies. Song et al. [129] showed computationally that on quasi-Mn-BTC, Eley-Rideal and Langmuir-Hinshelwood mechanisms compete. In the “fast reaction”, which proceeds via the LH mechanism, the N–H bond of NH₃ is first cleaved off on a Lewis acid site. Upon a

quick formation of NH₂NO, its conversion of HNNOH is the rate-determining step with a barrier of 0.79 eV, which later decomposes to H₂O and N₂. In the “standard mechanism”, which follows the ER pathway, the rate determining steps are the formation of NH₂NO from NH₂ and gaseous NO (0.73 eV) and its conversion to HNNOH (0.79 eV).

A similar competition of the two mechanisms was shown for Mn-Fe-BTC, as well [130].

2.3.3. Ceria-based and other oxide catalysts

W-doped CeO₂ was studied by Liu et al. [131], who calculated the entire reaction pathway. Using a simplified four-step catalytic cycle, the effect of W was shown to be beneficial. On MnCe_{1-x}O₂(111), a full mechanistic study revealed that NH₂ forms after the N-H dissociation of ammonia, which then forms NH₂NO upon adsorption of NO. Water desorption was identified as the rate determining step [132]. SO₄²⁻ can promote the reaction, was shown by Zhang et al. [133], who calculated the reaction pathway of NH₃ and NO in the presence of SO₄²⁻-CeO₂(111) sites.

To investigate SCR on bifunctional V_a-MnO_x catalysts, Xin et al. [134] constructed Mn₂O₃(202) and Mn₂V₂O₇(201) surfaces and investigated the entire reaction pathway, including NH₃ dissociation, the reaction with NO and N₂O. They confirmed that NH₂ plays a crucial role in the reaction. On Mn/γ-Al₂O₃, the calculated reaction rate determining barriers were 471.62, 281.25, and 341.55 kJ/mol [135].

A very thorough investigation of the SCR pathway on α-Fe₂O₃(012) was carried out by Gao et al. [136]. They investigated the standard NH₃-SCR reaction and found that the reaction follows the NO activation mechanism, forming NH₂NO and decomposing it into N₂ and H₂O. The first two are the rate-determining steps with barriers of 1.22 and 1.34 eV.

To recap, density functional theory calculations (DFT) were initially used to obtain the structures and electronic properties of the catalyst and the participating species. This included studying the adsorption of NH₃, NO₂, NO, O₂, N₂ and H₂O. On most catalysts, only NH₃ and H₂O exhibit a strong adsorption, while the other gases physisorb weakly and thus participate in the reaction via the Eley-Rideal mechanism. Rarely, such computations are employed to construct phase diagrams or to understand different IR or Raman spectra. Mechanistic studies have become prominent in the last decade, revealing the rate-determining steps and different pathways. When the calculated barriers range from 20 to 30 kcal/mol, the reactions are fast. In the NO activation mechanism, the formation of NH₂NO is usually the rate determining step, which is followed by a quick decomposition regardless of the catalyst.

3. Global kinetic and microkinetic modelling

For the ammonia SCR deNO_x reaction, most stationary kinetic models generally assume an Eley-Rideal (ER) mechanism, which implies the reaction between adsorbed NH₃ and the gas phase NO. Moreover, the adsorption equilibrium of ammonia and water at the active sites is assumed (competitive adsorption). The expression for the reaction rate considering the equation for site balance is [45]:

$$r = \frac{kK_{\text{NH}_3}C_{\text{NH}_3}C_{\text{NO}}}{1 + K_{\text{NH}_3}C_{\text{NH}_3} + K_{\text{H}_2\text{O}}C_{\text{H}_2\text{O}}} \quad (3.1)$$

where r , k , K_i and C_i are the reaction rate, the intrinsic chemical rate constant, the adsorption equilibrium constant of species i and the gas phase concentration of species i , respectively.

However, adsorption of water on the active sites is usually not considered in kinetic models (see Refs. [137–139]).

The other type of kinetic models is based on the Langmuir-Hinshelwood (LH) mechanism, which assumes a bimolecular reaction involving two co-adsorbed molecules (e.g. NH₃ and NO) on the surface. These kinetic models take into account the weak adsorption of the NO molecules on the catalyst surface, which occurs at low temperatures (<200 °C) [137].

3.1. Kinetic models of commercial V₂O₅-WO₃-TiO₂ catalysts

Yun and Kim [46] used the global kinetic model including standard,

fast, and NH₃ oxidation reactions with the Langmuir-Hinshelwood (LH) mechanism to predict the conversion of NO_x. The reactions and reaction rate expressions are summarized in Table 1.

The terms in the denominators of the reaction rate expressions in Table 1 take into account the inhibitory effects of surface coverage of the species.

The rate constants (k) and adsorption constants (K) both follow the Arrhenius-type expressions:

$$k_i = a_i e^{\frac{-E_i}{RT}} \quad (3.2)$$

$$K_i = A_i e^{\frac{-E_i}{RT}} \quad (3.3)$$

The authors used the commercial one-dimensional BOOST (AVL) code, as part of the gas exchange and cycle simulation, with the optimized reaction constants [46].

Shin et al. [137] developed a kinetic model for the selective catalytic reduction of nitrogen oxides based on the Eley-Rideal (ER) mechanism, using the equation-based modelling tool gPROMS® ProcessBuilder®. It was employed to evaluate the kinetic model by extracting intrinsic kinetic parameters from the experimental data collected in a conventional fixed-bed reactor. The modelling was performed considering all possible relevant catalytic reactions at SCR catalysts (Table 2), which can be classified into three groups: NO_x reduction (reaction numbers 1–3), NH₃ oxidation (reaction numbers 4–7) and accompanying reactions (gas-phase thermal reactions; reaction numbers 8–10).

NH₃ oxidation with lattice oxygen is expected to occur at relatively high temperatures. The model is a dual-site model: NO and NO₂ were assumed to compete with O₂ for the same adsorption site, while NH₃ adsorbs on a different site, as indicated by the rate expressions in Table 2. The reaction order with respect to O₂ (n) was estimated for the additional homogeneous gas-phase reactions.

The rate (k) and adsorption (K) constants were defined as:

$$k_i = k_{i,\text{ref}} e^{\frac{-E_i}{R} \left(\frac{1}{T} - \frac{1}{T_{\text{ref}}} \right)} \quad (3.4)$$

$$K_i = K_{i,\text{ref}} e^{\frac{-\Delta H_i}{R} \left(\frac{1}{T} - \frac{1}{T_{\text{ref}}} \right)} \quad (3.5)$$

3.2. Kinetic models of commercial Fe-zeolite catalysts

Metkar et al. [138] performed a comprehensive experimental and modelling study of the selective catalytic reduction of NO_x with NH₃ over Fe-ZSM-5 and Cu-chabazite (CHA) catalysts; only the modelling of SCR of nitrogen oxides over the Fe-ZSM-5 catalyst is described here. They developed a global kinetic model for the NO_x reduction reactions that occur during NH₃-SCR. Their model assumes a first-order dependence on the reactants, with some exceptions e.g. for the standard SCR reaction. The advantage of this model is the smaller number of kinetic parameters, but it lacks a mechanistic sophistication. The chemical reactions and their rate equations are listed in Table 3.

The definition of the rate constants (equation (3.2)) is the same as in the model of Yun and Kim [46].

Ammonia was assumed to adsorb on sites S , which can be considered as Brønsted acid sites. A coverage dependent desorption activation energy was assumed. The denominator in the rate expression for the standard SCR reaction (reaction number 4 in Table 3) explains the observed ammonia inhibition at lower temperatures. It is worth noting that several side reactions produce byproducts. One important byproduct is ammonium nitrate (NH₄NO₃), which is formed in the presence of excess NO₂. The formation of ammonium nitrate is particularly important at lower temperatures (<250 °C). It is assumed that the active sites of the catalyst are either free or have adsorbed ammonia. The rate expressions do not contain an explicit dependence on the concentrations of O₂ and H₂O.

Table 1

Reactions and rate expressions in the global kinetic model of Yun and Kim [46].

Number	Reaction	Rate expression
1	$4\text{NH}_3 + 4\text{NO} + \text{O}_2 \rightarrow 4\text{N}_2 + 6\text{H}_2\text{O}$	$\frac{kC_{\text{NH}_3}C_{\text{NO}}C_{\text{O}_2}}{T(1 + K_{\text{NO}}C_{\text{NO}} + K_{\text{H}_2\text{O}}C_{\text{H}_2\text{O}})^2(1 + K_{\text{NH}_3}C_{\text{NH}_3})^2(1 + K_{\text{O}_2}C_{\text{O}_2})^2}$
2	$4\text{NH}_3 + 2\text{NO} + 2\text{NO}_2 \rightarrow 4\text{N}_2 + 6\text{H}_2\text{O}$	$\frac{kC_{\text{NH}_3}C_{\text{NO}}C_{\text{NO}_2}}{T(1 + K_{\text{NO}}C_{\text{NO}} + K_{\text{H}_2\text{O}}C_{\text{H}_2\text{O}})^2(1 + K_{\text{NH}_3}C_{\text{NH}_3})^2}$
3	$4\text{NH}_3 + 5\text{O}_2 \rightarrow 4\text{NO} + 6\text{H}_2\text{O}$	$\frac{kC_{\text{NH}_3}C_{\text{NO}_2}}{T(1 + K_{\text{NO}}C_{\text{NO}} + K_{\text{H}_2\text{O}}C_{\text{H}_2\text{O}})^2(1 + K_{\text{NH}_3}C_{\text{NH}_3})^2(1 + K_{\text{O}_2}C_{\text{O}_2})^2}$

Symbols: T – temperature, A, a – pre-exponential factor, E – activation energy, R – universal gas constant.**Table 2**

Reactions and rate expressions in the kinetic model of Shin et al. [137].

Number	Reaction	Rate expression
1	$4\text{NH}_3 + 4\text{NO} + \text{O}_2 \rightarrow 4\text{N}_2 + 6\text{H}_2\text{O}$	$\frac{kK_{\text{NH}_3}P_{\text{NH}_3}K_{\text{O}_2}P_{\text{O}_2}P_{\text{NO}}}{(1 + K_{\text{NH}_3}P_{\text{NH}_3})(1 + K_{\text{O}_2}P_{\text{O}_2} + K_{\text{NO}}P_{\text{NO}} + K_{\text{NO}_2}P_{\text{NO}_2})}$
2	$6\text{NO} + 4\text{NH}_3 \rightarrow 5\text{N}_2 + 6\text{H}_2\text{O}$	$\frac{kK_{\text{NH}_3}P_{\text{NH}_3}P_{\text{NO}}}{(1 + K_{\text{NH}_3}P_{\text{NH}_3})}$
3	$2\text{NO}_2 + 4\text{NH}_3 + \text{O}_2 \rightarrow 3\text{N}_2 + 6\text{H}_2\text{O}$	$\frac{kK_{\text{NH}_3}P_{\text{NH}_3}K_{\text{O}_2}P_{\text{O}_2}P_{\text{NO}_2}}{(1 + K_{\text{NH}_3}P_{\text{NH}_3})(1 + K_{\text{O}_2}P_{\text{O}_2} + K_{\text{NO}}P_{\text{NO}} + K_{\text{NO}_2}P_{\text{NO}_2})}$
4	$4\text{NH}_3 + 3\text{O}_2 \rightarrow 2\text{N}_2 + 6\text{H}_2\text{O}$	$\frac{kK_{\text{NH}_3}P_{\text{NH}_3}K_{\text{O}_2}P_{\text{O}_2}}{(1 + K_{\text{NH}_3}P_{\text{NH}_3})(1 + K_{\text{O}_2}P_{\text{O}_2} + K_{\text{NO}}P_{\text{NO}} + K_{\text{NO}_2}P_{\text{NO}_2})}$
5	$4\text{NH}_3 + 5\text{O}_2 \rightarrow 4\text{NO} + 6\text{H}_2\text{O}$	$\frac{kK_{\text{NH}_3}P_{\text{NH}_3}K_{\text{O}_2}P_{\text{O}_2}}{(1 + K_{\text{NH}_3}P_{\text{NH}_3})(1 + K_{\text{O}_2}P_{\text{O}_2} + K_{\text{NO}}P_{\text{NO}} + K_{\text{NO}_2}P_{\text{NO}_2})}$
6	$2\text{NH}_3 + 8\text{NO} \rightarrow 5\text{N}_2\text{O} + 3\text{H}_2\text{O}$	$\frac{kK_{\text{NH}_3}P_{\text{NH}_3}P_{\text{NO}}}{(1 + K_{\text{NH}_3}P_{\text{NH}_3})}$
7	$4\text{NH}_3 + 4\text{NO} + 3\text{O}_2 \rightarrow 4\text{N}_2\text{O} + 6\text{H}_2\text{O}$	$\frac{kK_{\text{NH}_3}P_{\text{NH}_3}K_{\text{O}_2}P_{\text{O}_2}P_{\text{NO}}}{(1 + K_{\text{NH}_3}P_{\text{NH}_3})(1 + K_{\text{O}_2}P_{\text{O}_2} + K_{\text{NO}}P_{\text{NO}} + K_{\text{NO}_2}P_{\text{NO}_2})}$
8	$2\text{NO} + \text{O}_2 \rightarrow 2\text{NO}_2$	$k_{i,T_{\text{ref}}} e^{\frac{-E_i}{R} \left(\frac{1}{T} - \frac{1}{T_{\text{ref}}} \right)} C_{\text{NO}}^2 C_{\text{O}_2}^n$
9	$4\text{NH}_3 + 5\text{O}_2 \rightarrow 4\text{NO} + 6\text{H}_2\text{O}$	$k_{i,T_{\text{ref}}} e^{\frac{-E_i}{R} \left(\frac{1}{T} - \frac{1}{T_{\text{ref}}} \right)} C_{\text{NH}_3} C_{\text{O}_2}^n$
10	$4\text{NH}_3 + 3\text{O}_2 \rightarrow 2\text{N}_2 + 6\text{H}_2\text{O}$	$k_{i,T_{\text{ref}}} e^{\frac{-E_i}{R} \left(\frac{1}{T} - \frac{1}{T_{\text{ref}}} \right)} C_{\text{NH}_3} C_{\text{O}_2}^n$

Symbols: P_i – partial pressure of species i , T_{ref} – reference temperature, ΔH_i – adsorption enthalpy of species i .**Table 3**

Reactions and rate expressions in the global kinetic model of Metkar et al. [138].

Number	Reaction	Rate expression
1	$4\text{NH}_3 + \text{S} \leftrightarrow \text{NH}_3 \sim \text{S}$	$k_f X_{\text{NH}_3} \theta_v - k_b \theta_{\text{NH}_3}$
2	$2\text{NH}_3 \sim \text{S} + 1.5\text{O}_2 \rightarrow \text{N}_2 + 3\text{H}_2\text{O} + 2\text{S}$	$k_f X_{\text{O}_2} \theta_{\text{NH}_3}$
3	$\text{NO} + 0.5\text{O}_2 \leftrightarrow \text{NO}_2$	$k_f X_{\text{O}_2}^{0.5} X_{\text{NO}} - k_b X_{\text{NO}_2}$
4	$4\text{NH}_3 \sim \text{S} + 4\text{NO} + \text{O}_2 \rightarrow 4\text{N}_2 + 6\text{H}_2\text{O} + 4\text{S}$	$\frac{k_f X_{\text{NO}} \theta_{\text{NH}_3}}{1 + \frac{k_f}{k_b} X_{\text{NH}_3}}$
5	$2\text{NH}_3 \sim \text{S} + \text{NO} + \text{NO}_2 \rightarrow 2\text{N}_2 + 3\text{H}_2\text{O} + 2\text{S}$	$k_f X_{\text{NO}} X_{\text{NO}_2} \theta_{\text{NH}_3}$
6	$4\text{NH}_3 \sim \text{S} + 3\text{NO}_2 \rightarrow 3.5\text{N}_2 + 6\text{H}_2\text{O} + 4\text{S}$	$k_f X_{\text{NO}_2} \theta_{\text{NH}_3}$
7	$2\text{NH}_3 \sim \text{S} + 2\text{NO}_2 \rightarrow \text{N}_2 + \text{NH}_4\text{NO}_3 + \text{H}_2\text{O} + 2\text{S}$	$k_f X_{\text{NO}_2} \theta_{\text{NH}_3}$
8	$\text{NH}_4\text{NO}_3 \rightarrow \text{N}_2\text{O} + 2\text{H}_2\text{O}$	$k_f X_{\text{NH}_4\text{NO}_3}$
9	$2\text{N}_2\text{O} \rightarrow 2\text{N}_2 + \text{O}_2$	$k_f X_{\text{N}_2\text{O}}$
10	$2\text{NH}_3 \sim \text{S} + 3\text{N}_2\text{O} \rightarrow 4\text{N}_2 + 3\text{H}_2\text{O} + 2\text{S}$	$k_f X_{\text{N}_2\text{O}} \theta_{\text{NH}_3}$

Symbols: S – ammonia adsorption site, θ_i – fractional coverage of sites S , θ_v – fractional coverage of vacant sites S , X_i – mole fraction of species i , k_f – intrinsic chemical rate constant of the forward reaction, k_b – intrinsic chemical rate constant of the reverse reaction.

3.3. Kinetic models of commercial Cu-zeolite catalysts

Colombo et al. [139] developed a dynamic micro-kinetic model of the SCR deNO_x reactions. The rate parameters were estimated from the transient kinetic runs. The dual-site kinetic scheme includes acidic sites (*) for NH₃ adsorption and desorption (coverage is indicated by the symbol Theta) and sites associated with the Cu promoter of the zeolite catalyst (S-sites), where reaction steps (reaction numbers 2–8 in Table 4)

Table 4

Reactions and rate expressions in the micro-kinetic model of Colombo et al. [139].

Number	Reaction	Rate expression
1	$\text{NH}_3 \leftrightarrow \text{NH}_3^*$	$k_f C_{\text{NH}_3} \theta_v - k_b \theta_{\text{NH}_3}$
2	$2\text{NO}_2 + 2\text{S} \sim \text{OH} \leftrightarrow \text{S} \sim \text{ONO} + \text{S} \sim \text{NO}_3 + \text{H}_2\text{O}$	$k_f (C_{\text{NO}_2} \sigma_v)^2 - k_b \sigma_{\text{ONO}} \sigma_{\text{NO}_3}$
3	$\text{NO}_2 + \text{S} \sim \text{ONO} \leftrightarrow \text{NO} + \text{S} \sim \text{NO}_3$	$k_f C_{\text{NO}_2} \sigma_{\text{ONO}} - k_b C_{\text{NO}} \sigma_{\text{NO}_3}$
4	$\text{S} \sim \text{NO}_3 + \frac{1}{2} \text{H}_2\text{O} \rightarrow \text{NO}_2 + \frac{1}{4} \text{O}_2 + \text{S} \sim \text{OH}$	$k \sigma_{\text{NO}_3}$
5	$\text{S} \sim \text{ONO} + \text{NH}_3^* \rightarrow \text{N}_2 + \text{H}_2\text{O} + \text{S} \sim \text{OH}$	$k \theta_{\text{NH}_3} \sigma_{\text{ONO}}$
6	$\text{S} \sim \text{NO}_3 + \frac{2}{3} \text{NH}_3^* \rightarrow \text{S} \sim \text{ONO} + \frac{1}{3} \text{N}_2 + \text{H}_2\text{O}$	$k \sigma_{\text{NO}_3} \theta_{\text{NH}_3}$
7	$\text{S} \sim \text{NO}_3 + \text{NH}_3^* \leftrightarrow \text{S} \sim \text{NO}_3[\text{NH}_3]$	$k_f \theta_{\text{NH}_3} \sigma_{\text{NO}_3} - k_b \sigma_{\text{NO}_3}[\text{NH}_3]$
8	$\text{S} \sim \text{NO}_3[\text{NH}_3] \rightarrow \text{N}_2\text{O} + \text{H}_2\text{O} + \text{S} \sim \text{OH}$	$k \sigma_{\text{NO}_3}[\text{NH}_3]$
9	$2\text{NH}_3^* + 2\text{NO}_2 \rightarrow \text{NH}_4\text{NO}_3^* + \text{N}_2 + \text{H}_2\text{O}$	$\frac{k \theta_{\text{NH}_3} C_{\text{NO}_2}^2}{1 + K_{\text{NH}_4\text{NO}_3} \theta_{\text{NH}_4\text{NO}_3}}$
10	$\text{NH}_4\text{NO}_3^* \rightarrow [\text{NH}_3 + \text{HNO}_3] \rightarrow \text{NH}_4\text{NO}_3$	$k \theta_{\text{NH}_4\text{NO}_3}$
11	$\text{NH}_4\text{NO}_3^* \rightarrow \text{N}_2\text{O} + 2\text{H}_2\text{O}$	$k \theta_{\text{NH}_4\text{NO}_3}$
12	$\text{NO} + \frac{1}{2} \text{O}_2 \leftrightarrow \text{NO}_2$	$\left\{ k \left[C_{\text{NO}} (P_{\text{O}_2})^{0.5} - \frac{C_{\text{NO}_2}}{K_{\text{eq-NO}}} \right] \right\} \left(\frac{P_{\text{H}_2\text{O}}}{0.03} \right)^\theta$
13	$\frac{3}{2} \text{NO} + \text{NH}_3^* \rightarrow \frac{5}{4} \text{N}_2 + \frac{3}{2} \text{H}_2\text{O}$	$k \theta_{\text{NH}_3} C_{\text{NO}}$

Symbols: * – acidic site, S – Cu promoter site, θ_i – fractional coverage of sites i , σ_i – fractional coverage of S sites, $K_{\text{eq-NO}}$ – chemical equilibrium constant defined in Ref. [139].

involving nitrites/nitrates are expected (coverage is indicated with the symbol sigma).

The kinetic mechanism in Table 4 explicitly accounts for the differences in the formal oxidation state of nitrogen in both gaseous and surface NO_x species. The oxidation state of the catalytic sites (S–OH) is assumed to be invariant because the strong oxidizing conditions associated with the presence of NO₂ likely maintain the Cu-sites in their highest oxidation state.

Additional global reactions were also included in the model to better describe the reaction system: ammonium nitrate formation, sublimation and decomposition to N₂O (reactions 9–11 in Table 4), reversible NO oxidation to NO₂ (reaction 12 in Table 4), and the slow SCR reaction (reaction 13 in Table 4).

It should be noted that all kinetic runs reported in this study were performed in the absence of oxygen in the feed stream to avoid interference with the standard SCR and the NO and ammonia oxidation reactions.

Shibata et al. [140] developed a simple kinetic model for the standard NH₃-SCR reaction with Cu-ZSM-5 catalyst, considering only three reaction steps: NH₃ adsorption (and desorption), NH₃ oxidation and the standard SCR reaction. Their model was validated with the experimental results, which had not been considered in the estimation of the model.

Global kinetic and microkinetic models of SCR deNO_x processes are usually based either on the Eley-Rideal (ER) or on the Langmuir-Hinshelwood (LH) reaction mechanisms. The models usually consider one or two types (dual-site models) of adsorption sites and from 3 up to

13 reactions. Some of the studied kinetic models also predict the formation of intermediates in form of nitrites and/or nitrates (e.g. ammonium nitrate). However, most of kinetic models available in the literature do not account for the adsorption of water molecules on the active sites of SCR deNO_x catalysts.

4. CFD simulations

The kinetic model of Shin et al. [137] (described in chapter 3.1.; Table 2) and the estimated parameters were summarized in the form of a user-defined function (UDF) used in a commercial computational fluid dynamics (CFD) package, ANSYS® Fluent®, to search for an optimized SCR monolith channel geometry.

The 3D model of a channel for the SCR honeycomb catalyst had a length of 450 mm (Fig. 5), which is the commonly observed length of commercial SCR monoliths. To save computational time, accounting for the symmetry of the monolith cross-section, only a quarter of the monolith channel was modelled.

The reaction kinetic parameters obtained from the fixed-bed experiments were converted into a surface reaction model, which was applied to the surface zones of the monolith catalyst of the CFD simulation. The gas-phase and the catalytic reaction rate equations were implemented as two UDFs written in C and dynamically linked to the ANSYS Fluent solver.

The CFD calculations were performed with constant velocity inlet boundary conditions for the gas mixture. The outlet pressure was set to the atmospheric pressure. The catalyst wall was set to a constant reaction temperature. The Reynolds numbers of the flow were in the laminar range (500–800).

Square and rectangular channel geometries (with different aspect ratios B/A) were tested for pressure drop and NO conversion (Fig. 7). The width of the channel is denoted by A, while the wall thickness C was kept at 0.7 mm (Fig. 6).

The relative NO conversion and pressure drop on the ordinate axes of Fig. 7 were defined as the ratio of NO conversion and pressure drop of the rectangular channel to those of the square channel. As the aspect ratio of the rectangular channel is increased, both the pressure drop and NO conversion decrease, so there is a tradeoff between these the two factors in choosing the optimal size and geometry of the channel. The aspect ratios that are practical for commercial production are in the range of 1–5 [137].

Since rectangular channels have 90° angles at the corners, they can affect monolith performance by reducing chemical conversion, increasing pressure drop and increasing susceptibility to plugging and scaling (when particles are present in the flue gas stream). To mitigate these problems, an elongated hexagonal channel (with an angle of 120°) was tested using the CFD methodology. With a channel width of 3.2 mm and an aspect ratio of 2.5, the elongated hexagonal channel exhibited a 3.5% lower pressure drop while maintaining the same degree of NO conversion. This can be explained by comparing the velocity field distributions in the rectangular and hexagonal channels: the higher portion of the rectangular cross-section has lower velocities than its elongated hexagonal counterpart (under the same boundary conditions). The regions of low flow velocities of the rectangular channel are located near the catalyst surface, resulting in inefficient use of the channel space for

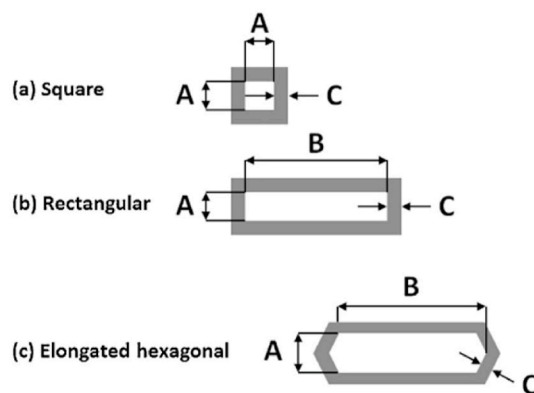


Fig. 6. The tested different monolith cross-sections with symbols (A, B and C) for their characteristic dimensions [137]. © 2019 Institution of Chemical Engineers. Published by Elsevier B.V.

catalytic reactions.

The steady-state application of the NH₃-SCR deNO_x process in a coal-fired power plant was modelled considering only the standard SCR reaction and the reaction of ammonia oxidation, which were inserted into the UDF used with the CFD simulation in the ANSYS Fluent software package. The catalyst used was the commercial V₂O₅-WO₃/TiO₂ honeycomb catalyst. Zhou et al. [141] studied the instantaneous velocity distributions and ammonia slip in their 3D model of a SCR system and suggested some changes to the geometry of the elements of the system.

There are not many articles published on the CFD simulations of the NH₃-SCR deNO_x process itself. On the other hand, there are many CFD studies [142–144] on the injection of urea-water solution (UWS) into SCR deNO_x systems. Three-dimensional (3D) numerical simulations of vanadia monolith honeycomb catalysts can also be found in the literature. Roduit et al. [145] used finite-element methods programmed in Matlab V to investigate the flow, mass transfer, and chemical reaction processes (Eley-Rideal (ER) mechanism for the standard SCR reaction and the NH₃ oxidation side reaction) in a honeycomb catalyst to calculate the distribution of NO concentration in the catalyst wall. Zheng et al. [146] also developed a three-dimensional model combining the selective catalytic reduction (standard SCR reaction) of NO with ammonia and SO₂ oxidation reactions over a monolithic honeycomb catalyst to investigate the effects of catalyst structure and operating parameters on NO reduction and SO₂ oxidation.

The CFD modelling approaches usually incorporate the SCR deNO_x chemical reactions by the user-defined functions (UDFs) and couple them with the mass transport phenomena associated with fluid flow through the monolith catalyst channels. Most of the CFD modelling is done using commercial CFD software packages. The fluid flow conditions are typically in the laminar regime and at least with conventional channel designs there is a trade-off between the pressure drop and the NO_x conversion performance. The literature on CFD modelling of NH₃-SCR deNO_x processes is scarce, while there are many CFD studies on the injection of urea-water solution (UWS) into SCR deNO_x systems.

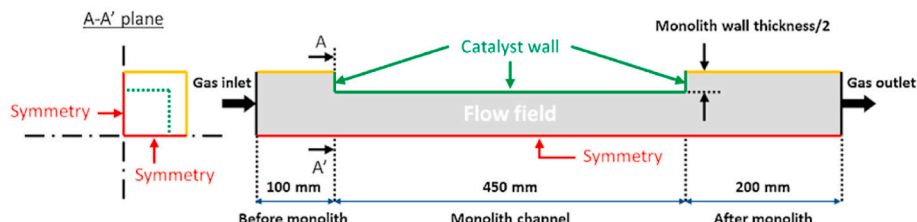


Fig. 5. Schematic representation of the 3D model of the single monolith channel [137]. © 2019 Institution of Chemical Engineers. Published by Elsevier B.V.

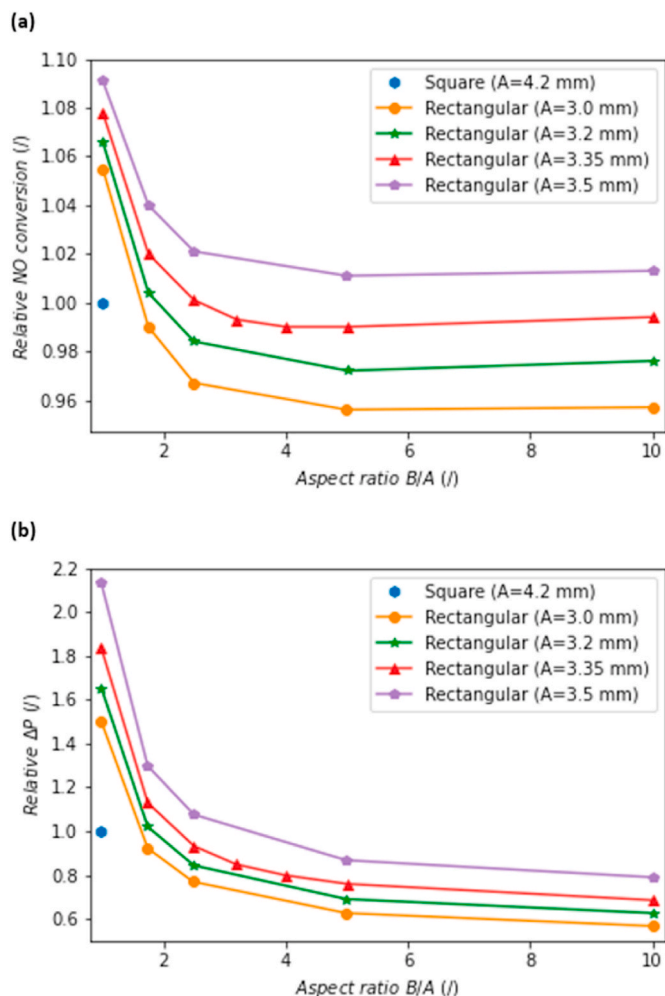


Fig. 7. Performance comparison between a square and a rectangular channel with the same wall thickness (0.7 mm): (a) relative NO turnover and (b) relative pressure drop. Inlet boundary conditions: 1500 ppm NO, 1500 ppm NH₃, 0.5 vol % H₂O, 13.5 vol% O₂ and N₂ equilibrium at 5 m/s and 350 °C. Adapted from Ref. [137]. © 2019 Institution of Chemical Engineers. Published by Elsevier B.V.

5. Conclusions

With recent advances in computational methods and available computing power, periodic first-principles models are increasingly being used to gain additional insight into the reaction mechanism. However, most experimental studies still incorporate DFT considerations that are, at best, tentatively linked to the experiments. In most cases, DFT studies deal with adsorption of ammonia and other reactants and products. Comprehensive mechanistic studies that would offer promising insights into reaction mechanism and kinetics remain relatively rare. When they are performed, they are purely theoretical studies with little to no experimental support. This represents an important gap between the state of the art of computations and experimental work,

Appendix A. Properties of hydrogen and ammonia as fuels

Hydrogen as a fuel has low minimum ignition energy (0.02 mJ), wide ignition limits (4.1–75% in air) and high flame propagation rate (stoichiometric laminar flame velocity of 270 cm/s). Therefore, it could be more dangerous than gasoline or natural gas [147]. The adiabatic flame temperature of hydrogen is 2384 K (2111 °C). The average temperature and NO_x emissions in an axisymmetric small burner were 1268 K and 562 ppm, respectively. For conventional combustion of hydrogen, the predicted maximum NO_x was 1961 ppm and the predicted maximum temperature was about 2325 K; therefore, local temperatures and NO_x concentrations vary by site [148]. Hydrogen emits up to 5000 ppm of NO_x [149].

offering a promising avenue for further research. Most importantly, reasonable structural models are essential for high quality and useful DFT calculations. Since the catalyst is an active and constantly changing system during the reaction, this is a daunting task. A naive way to solve this problem is to find an “average” catalyst structure and construct an atomistic approximation of the catalyst structure. While this provides useful results, it is not sufficient to provide a complete mechanistic description of a functioning catalyst.

Nevertheless, the present studies are also useful for catalyst screening for targeted improvement. In the future, the increasing accuracy of DFT studies will allow them to be used for prediction, design and selection of active catalyst materials with desired properties. Here, the resistance to hydroxylation and water poisoning is the most pressing issue, as this has been repeatedly shown to be the rate-determining step in the reaction and thus acts as a bottleneck to the overall catalyst performance.

Most kinetic models in the literature do not account for the adsorption of water molecules on the catalysts. Therefore, it is not possible to predict the conversion performance of the catalysts at higher water vapor content using this group of models. In contrast, the global kinetic model of Yun and Kim [46] considered the adsorption of water vapor on the active sites of the commercial V₂O₅-WO₃-TiO₂ catalyst and showed a significant reduction of the performance in the lower temperature range of the catalyst even at a H₂O content of 10 vol% in the feed gases.

The CFD modelling approach usually considers chemical reactions within the user-defined function/s (UDF/s) and couples it/them with mass transport phenomena associated with the fluid flow through the catalyst, which is done in commercial CFD software packages (e.g. ANSYS Fluent). The development of the detailed CFD methodology could also model processes of adsorption and desorption of species (e.g. ammonia and water) on the catalyst.

During the literature review, the authors identified a large knowledge gap on the topic of NH₃-SCR deNO_x from flue gases with high water vapor content (>15 vol%) produced after hydrogen or ammonia combustion. This gap has been identified in terms of both experimental results and modelling. We see a great need for investigations of the SCR deNO_x process of flue gases with high water content.

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Declaration of competing interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

Data availability

Data will be made available on request.

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The combustion characteristics of ammonia are: high minimum ignition energy (8 mJ [150]), narrow ignition limits (16–25% by volume in air [151]), low flame propagation rate (laminar flame velocity of 7 cm/s [152]) and relatively low adiabatic flame temperature (lower than hydrogen; 2050 K - 1777 °C [153]). Combustion of ammonia with air produces about 2645 ppm NO_x with an equivalence ratio of 0.94 [154]. Plasma assisted combustion [154] and rich-lean staged combustion [155] can reduce NO_x emissions from ammonia combustion. Ammonia emits up to 2750 ppm of NO_x [149].

Some researchers also studied the combustion of mixtures of the two fuels. The combustion of hydrogen-ammonia mixtures was studied by [155] and [153].

Appendix B. Combustion reactions of hydrogen and ammonia and composition of their combustion products

The heat of combustion of hydrogen under standard conditions is −285.8 kJ/mol, while for ammonia it is −382.8 kJ/mol. The energy density of hydrogen is 141.8 kJ/g or 11.68 kJ/dm³ (at 101325 Pa, 25 °C), while ammonia has values of 22.48 kJ/g and 15.65 kJ/dm³ (at 101325 Pa, 25 °C).



Combustion products at various equivalence ratios (ER) are listed in Tables B1 and B.2. Note that the formation of nitrogen oxides during the combustion of hydrogen and ammonia is not considered here.

Table B.1

Composition of the combustion products after the combustion of hydrogen with air.

ER	H ₂ (vol%)	H ₂ O (vol%)	O ₂ (vol%)	N ₂ (vol%)
0.75	10.4	31.1	0.0	58.5
0.80	8.0	31.9	0.0	60.1
0.85	5.8	32.7	0.0	61.5
0.90	3.7	33.4	0.0	62.9
0.95	1.8	34.1	0.0	64.1
1.00	0.0	34.7	0.0	65.3
1.05	0.0	33.3	0.8	65.8
1.10	0.0	32.1	1.6	66.3
1.15	0.0	30.9	2.3	66.8
1.20	0.0	29.8	3.0	67.2
1.25	0.0	28.8	3.6	67.6

Symbols: ER - equivalence ratio.

Table B.2

Composition of the combustion products after the combustion of ammonia with air.

ER	NH ₃ (vol%)	H ₂ O (vol%)	O ₂ (vol%)	N ₂ (vol%)
0.75	6.5	29.1	0.0	64.4
0.80	4.9	29.6	0.0	65.5
0.85	3.5	30.0	0.0	66.5
0.90	2.3	30.4	0.0	67.3
0.95	1.1	30.8	0.0	68.1
1.00	0.0	31.1	0.0	68.9
1.05	0.0	30.0	0.8	69.3
1.10	0.0	29.0	1.4	69.6
1.15	0.0	28.0	2.1	69.9
1.20	0.0	27.1	2.7	70.2
1.25	0.0	26.3	3.3	70.5

Symbols: ER - equivalence ratio.

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